# CENTRIPETAL FORCE FROM GRAVITY 

Unit 14 \& some 8 Dr. John P. Cise, Professor of Physics, Austin Com. College, 1212 Rio Grande St., Austin Tx. 78701 jpcise@austincc.edu \& New York Times, September 15, 2016 by Jonah Engel Bromwich \& Nicholas St. Fleur

## Why Pluto's Moon Charon Wears a Red Cap



The red cap on the north pole of Charon, the largest of Pluto's moons.
It turns out that Pluto may be responsible for maintaining the highlights on the red head of its biggest moon. Scientists think Pluto, which was consigned to underdog status when it was demoted to a dwarf planet a decade ago, may actually be more of a bully. Data published in the journal Nature on Wednesday reinforced the theory that Pluto's atmosphere is releasing gas captured near Charon's frigid northern pole, forcing the largest of its five moons to wear a blotchv, reddish-brown dunce cap. He said the color would be familiar to those who used to travel to Los Angeles when the city was more polluted. "Back in the old days when you'd fly into Los Angeles, there'd be a sea of this orangeybrown muck," he said. "That's basically light hydrocarbons that are the product of human activity - like the of people's gas tanks - being affected by ultraviolet light from the sun," a chemical process similar to the one occurring on Charon. Scientists theorize that Pluto and Charon were formed by the same collision some four and a half billion years ago. And while Pluto's radius is nearly twice the size of Charon's, their centers are about 11,800 miles apart, a distance so comparatively small that they move in a lock step rare for celestial bodies, each keeping the same face directed toward its mate at all times.
INTRODUCTION: Goal here is to find orbit speed of Charon around center of mass. The radius R of Charon's orbit is needed to solve for $v$ by using gravity providing centripetal force: $G m M / R^{2}=m v^{2} / R$. Thus, $[G M / R]^{1 / 2}=v$ eq. $1 \quad M=$ mass of Pluto + Charon combined $=13 \times 10^{21} \mathrm{~kg} .+1.586 \times 10^{21} \mathrm{~kg} .=14.586 \times 10^{21} \mathrm{~kg} . \mathrm{R}$ can be found as it is the distance from center of mass( cm ). Let $X=$ distance cm is from center of Pluto. The cm can be found using cm finding equation $X=\Sigma \mathrm{xm} / \Sigma \mathrm{m}$. Take $(0,0)$ to be at center of Pluto. Distance between Pluto and Charon is given in the article above as 11,800 miles.

QUESTIONS: (a) Convert 11,800 miles to meters?, (b) Find X? Distance cm is from center of Pluto? (c) Find orbit $\mathbf{R}$ radius of Charon. $\mathrm{R}=\mathbf{1 1 , 8 9 9}$ miles(in meters) $\mathbf{- X}$, (d) Find orbital speed v of Charon?

HINTS: $\mathbf{G}=$ gravitational constant $=6.67 \times 10^{-11} \mathrm{~N} \mathrm{~m}^{2} / \mathrm{kg}^{2}$, mile $=1609$ meters
ANSWERS: (a) $18.986 \times 10^{6} \mathrm{~m}$., (b) $2.063 \times 10^{6} \mathrm{~m}$., (c) $R=16.911 \times 10^{6} \mathrm{~m}$, (d) $\mathrm{v}=\sim 2.4 \times 10^{2} \mathrm{~m} . / \mathrm{s}$. or $0.24 \mathrm{~km} . / \mathrm{s}$. NOTE: Computed orbit speed $v$ of Charon is just a little short reported by NASA and Wikipedia. Dr. Cise

